

sources, being solar photovoltaic (PV) or micro-wind turbine, or by micro gas turbine. In particular, this work uses historical data of weather (in the form of actual solar PV and wind power generation), central power generation, and electrical energy demands, from Australia of 2010, thus providing a realistic simulation environment for both demand and renewable generation.

The aims of this work are two-fold: (a) To determine the composition of the power network in terms of the type, number and location of the non-central DG units, with the goal of finding the cheapest configuration (capital cost), of meeting demand for power while keeping over- and under-production of power as low as possible, and of minimizing the spot price and CO₂ emissions, thus determining the best, or at least high performing candidate network solutions; (b) To analyse the multi-dimensional results of the evolutionary computation component in order to reveal relationships between the network's design vector elements, by means of most influential nodes and type of technology, as well as tipping points in the behaviour of the system.

Procedure

Background

The Plexos tool⁹ is incorporated to provide both OPF and financial market simulations, in particular providing unit commitment (which generators should be used, bearing in mind their operating characteristics such as ramp-up time as well as power output and running costs), economic dispatch (which generators to use to meet demand from a cost viewpoint), transmission analyses (losses, congestion), and spot market operation. It also provides estimations of CO₂ emissions. The volume of lost load (VoLL) is the threshold price above which loads prefer to switch off, while the dump energy price is that below which generators prefer to switch off, and these along with market auctions also contribute to the ratio of power generated to power consumed. Transmission losses are also taken into account within Plexos through sequential linear programming.

Plexos is integrated with a multi-objective optimizing evolutionary algorithm (MOOEA)¹⁰, thus establishing an optimization feedback loop, since Plexos gives optimal unit commitment for a given set of DG units, while the MOOEA is used to determine the optimal set of generators for the given demand profile and weather pattern. A MOOEA is used as they have a history of tackling non-linear¹¹ multi-objective and multi-dimensional optimization problems successfully, and since OPF for AC power is a non-linear problem while power markets require multi-part non-linear pricing. In the model used here, there are seventy two parameters that constitute the design vector applicable to each candidate solution, represented as one individual in the MOOEA, thus the problem is both non-linear and multi-dimensional. The simulation has a horizon of one calendar year, represented as 365 steps of 1 day increments with a resolution to 30 minutes, from 01-Jan-2010.

A MOOEA¹² is generally an heuristic, stochastic means of searching very large non-linear decision or objective spaces in order to attempt to obtain (near) optimal or high-performing solutions¹³ for problems upon which classical optimization methods do not perform well. EAs are characterized by populations of potential solutions that converge towards local or global optima through evolution by algorithmic selection as inspired by neo-Darwinian¹⁴ evolutionary processes. An initial population of random solutions is created and through the evaluation of their fitnesses for selection for reproduction, and by the introduction of variation through mutation and recombination (crossover), the solutions are able to evolve towards the optima.

MOO gives rise to a set of trade-off solution points¹⁵ since all objectives are optimised simultaneously, giving rise to individuals that cannot be improved upon in one objective function (OF) dimension without being degraded in another. When each remaining solution in the population cannot be said to be better than any other in *all* OF dimensions, they are called non-dominated and are members of the local Pareto-optimal set, and are all of equal value and potential interest to the researcher. The non-dominated set of the entire feasible search space is the global Pareto-optimal set¹².

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Fig. 2: IEEE 30-bus test system

The IEEE 30-bus test system in single line diagram style¹⁶, showing the location of DG units by bus (node) as numbered in large bold. The V-number is that of the variable holding the number of DG units assigned for the associated DG type at that bus as cross-referenced in Table 1. The circle with tilde indicates a large central generator input and the down arrow indicates bus output to a load.

Method

The evolutionary algorithm used here is a multi-objective optimizing genetic algorithm that self-adapts its control parameters, where the term self-adaptive is used in the sense of Eiben *et al.*¹⁷ following on from the work of Bäck¹⁸, to indicate control parameters that are encoded in the internal representation of each candidate solution along with the problem definition parameters applying to the objective functions (the *main* parameters), and that these control parameters are subject to change along with the *main* parameters due to mutation and crossover. This is different from a purely *adaptive* control parameter strategy as in that case the change is instigated algorithmically by some feedback at the higher level of the genetic algorithm (GA) rather than the lower level of each chromosome/solution in the population. The *deterministic* approach is rule-based and is not considered adaptive.

The Plexos tool is used here as the source of the values of the objective functions that are evaluated and selected for, that is to say, the fitness indicators, by the MOOEA, as depicted in Figure 3.

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Fig. 3: MOOEA

The integration of Plexos with the self-adaptive multi-objective optimization algorithm.

The problem is defined as a set of potential DG units each of which may or may not be located at a given node (bus). The DG units are defined as (i) micro-gas turbine (ii) Wind turbine and (iii) Solar photovoltaic, where a unit of value 0 means the generator is not present at the location. The scenario allows for up to 5 units of each type to be located at any of the nodes defined as variable in the network diagram (Figure 2), which means that it is any except for the nodes 1, 2, 13, 22, 23 and 27, as these are the large fixed central OCGT power stations.

The labels shown as V_n at the given nodes indicate the design variable number that defines the number of units of the given generator types at that bus, and as can be seen, each of the 3 variable types can be present potentially. As there are 24 nodes at which variable DG units can be located and 3 types of generator, the design vector of each candidate solution therefore consists of 72 variables. A candidate solution is therefore a vector of n decision variables: $=(x_1, x_2, \dots, x_n)$, where $n = 72$. This configuration thus allows a solution to have from 0 DG units up to a theoretical 360 (being 5 units of each of 3 DG types at the 24 nodes). Table 1 below shows the allocation of DG units by type to nodes, cross-referenced to its variable number (as shown in Figure 2), with the assumption that a given generator feeds in to one associated node only.

There are 4 objective functions defined, all of which are to be minimised simultaneously and the values for all of which come from Plexos, these being:

$$\text{Eq. 1 } \min F(\text{genCost}) = \text{genCost}$$

$$\text{Eq. 2 } \min F(\text{useDump}) = | \text{useDump} |$$

$$\text{Eq. 3 } \min F(\text{spotPrice}) = \text{spotPrice}$$

$$\text{Eq. 4 } \min F(\text{CO}_2) = \text{CO}_2$$

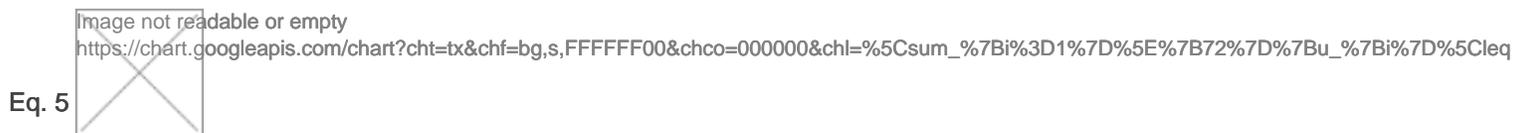
in which the values represent respectively:

- The generation cost (in currency, e.g. \$)
- The USE/DUMP energy (MWh)
- Spot Price (\$/MWh)
- CO₂ emissions (Kg)

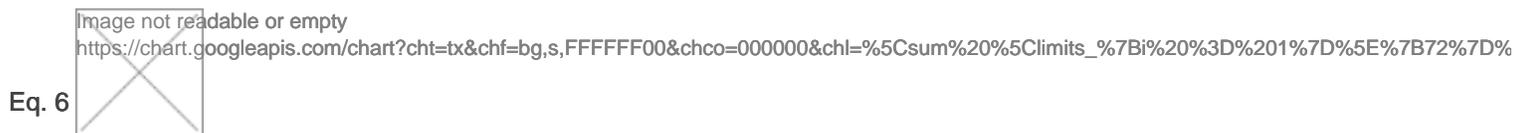
Considering the values above, useDump, depending upon whether it is negative or positive, is respectively either the un-served amount of energy due to under-production or the dump energy due to over-production, relative to demand. By minimizing the absolute value of useDump, the optimization seeks to make this value approach zero, that is to say, to try to make the supply match the demand, thus obtaining the most efficient system. The spot price is the mean price achieved in the simulated market

auctions over the course of the simulation, in Plexos.

A hard constraint, $sumU$, on the total number of DG units deployed, u , is applied in Equation 5, in order to investigate how the system transforms itself. Without such a constraint, which can be viewed as a limit to financial resources available as investment into DG, we would perhaps expect the system to maximize DG deployment since they provide a known benefit and where cost is the only downside, and this would hide the effects that placement may have when otherwise.



The hard constraint is increased in other runs to see what effect a larger number of allowed units may have, as shown in Equation 6:



The candidate solutions chosen by the MOOEA, using the results from Plexos, are thus selected due to the effect their chosen DG units have on the electrical network due to their operating characteristics and where they feed into the network, defined in the topology as shown in Figure 2.

The MOOEA allows each new experiment, such as the one defined here, to override its default initializer which creates an initial population of candidate solutions by generating variables under a uniform random distribution regime within the ranges of the defined variables, in this case $0 \leq u \leq 5$. The initializer used instead generates solutions that meet the hard constraint, by selecting for each solution a random value between 0 and the constraint, 70, and using this as the limit for that candidate solution. Each variable of that solution is then selected randomly, and is allocated a random value within its range, until the solution's own limit is reached. In this way, solutions in the initial population will vary between 0 DG units and 70 with a uniform distribution.

In subsequent generations, solutions will evolve that may break the hard constraint, due to mutation and recombination operators acting on 'fit' parent solutions selected for breeding, and in this case the solutions will be retained in the population but repaired. Repairing in this context means that a failing solution's vector of DG variables is changed until it falls within the constraint, by randomly choosing one of the variables, decrementing its DG unit count (when it has $u=1$), and then repeating the process until the total falls within the constraint.

The MOOEA is configured to have a mixed *chromosome* consisting of a vector (the *genes*) of 72 integers, with the self-adaptive control parameters encoded as real numbers. It has a fixed population of size 30, allows 0 duplicate solutions in any given generation, has initial crossover and mutation probabilities of 0.9 and 0.01389 ($= 1/72$) respectively and is allowed to run until all solutions are non-dominated or until 5 days have elapsed, whichever is sooner (since each generation takes in the region of 3 to 4 hours elapsed time, which increases as the generations increase, apparently).

Table 1

The nodes, their generators and generator types.								
Gas			Wind			Solar PV		
Node	DG	Var	Node	DG	Var	Node	DG	Var
n03	g02	V01	n03	g09	V02	n03	g10	V03
n04	g02	V04	n04	g09	V05	n04	g10	V06
n05	g02	V07	n05	g09	V08	n05	g10	V09
n06	g02	V10	n06	g09	V11	n06	g10	V12
n07	g02	V13	n07	g09	V14	n07	g10	V15
n08	g02	V16	n08	g09	V17	n08	g10	V18
n09	g02	V19	n09	g09	V20	n09	g10	V21
n10	g02	V22	n10	g09	V23	n10	g10	V24
n11	g02	V25	n11	g09	V26	n11	g10	V27
n12	g02	V28	n12	g09	V29	n12	g10	V30
n14	g02	V31	n14	g09	V32	n14	g10	V33
n15	g02	V34	n15	g09	V35	n15	g10	V36
n16	g02	V37	n16	g09	V38	n16	g10	V39
n17	g02	V40	n17	g09	V41	n17	g10	V42
n18	g02	V43	n18	g09	V44	n18	g10	V45
n19	g02	V46	n19	g09	V47	n19	g10	V48
n20	g02	V49	n20	g09	V50	n20	g10	V51
n21	g02	V52	n21	g09	V53	n21	g10	V54
n24	g02	V55	n24	g09	V56	n24	g10	V57
n25	g02	V58	n25	g09	V59	n25	g10	V60
n26	g02	V61	n26	g09	V62	n26	g10	V63
n28	g02	V64	n28	g09	V65	n28	g10	V66
n29	g02	V67	n29	g09	V68	n29	g10	V69
n30	g02	V70	n30	g09	V71	n30	g10	V72

Results

The results are given as 2D scatter plots and higher dimensional plots using the parallel coordinates (?-coords) technique^{19,20,21,22}, in which each dimension is oriented parallel to the others, thus transforming an n-D point into a polygonal line. The latter technique enables multivariate data to be plotted uniquely and without loss of information, and in these cases the whole design space of each solution, 72 variables, are plotted alongside their objective function results, and also with the sum of the DG units assigned ($sumU$) as in Equation 5.

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Fig. 4: Scatter plots of four OFs

Scatter plots showing $sumU$ on y-axis and (a) Top left: $genCost$ (b) Top right: $useDump$ (c) Bottom left: $spotPrice$ (d) Bottom right: CO_2 , and on the right a ?-coords plot showing a selected region of higher $sumU$ which corresponds to lower OF values. Hard constraint on $sumU = 70$.

Figure 4 concerns results obtained when the hard constraint of 70 was applied to $sumU$, and the scatter plots of show the $sumU$ plotted against the four OFs as described in Equation 1 through Equation 4, from which it can be seen that there is broadly a trade-off between the number of DG units deployed and the quality of each of the other OF values. An obvious optimal trade-off front has not yet developed in the course of the optimisation, but the trend is clear, and that is that increasing the number of DG units deployed improves (decreases) the other OF values. The ?-coords plot to the right of the scatter plots emphasises this point, in that there is a narrow region between $sumU$ and $genCost$ in which the lines from $sumU$ cross, itself an indication of anti-correlation, while the lines from $genCost$ to the other OFs to its right are mostly positively correlated. It can be seen however that not all of the lower $genCost$ points lead to the lower $useDump$ points, and indication that possibly a little more central generation was needed under certain circumstances, meaning that supply and demand was not always so well matched.

Also in Figure 4 in the ?-coords plot there is an indication that the system may have a tipping point (bifurcation) dependent upon the value of $sumU$ at around 34 units, as the selected region shown by the two arrows has an upper boundary of 34, and the OFs relating to all these lines seems to be in the top half of the worst performers.

The plots of Figure 6 and Figure 7 also related to the hard constraint of 70 units, and show the best performing solution found for the $genCost$ objective. The latter figure makes it clear that it is the wind turbine DG units (indicated by W) that are the primary contributor to the performance of the best solution for $genCost$, with variable V32 having the most units allocated, and V11 being the most connected in the network (feeding into node n06).

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Fig. 5: Hard constraint of 200

Shows results when the hard constraint $sumU$ is increased to 200, with scatter and ?-coords plots similar to Figure 4.

The results of Figure 5 are presented similarly to those of Figure 4, but for the hard constraint of 200. The ?-coord plot shows the relationship between the number of DG units and best performing OFs more clearly (when in colour), in that the more DG units allocated, the better the OF performance. Clearly, without the constraint the system would attempt to allocate as many DG units as possible, so the constraint acts as a limit on the cost of DG deployment. The scatter plots of $sumU$ against the OFs also show the clear trade-off trend.

Conclusion

It has been shown that this methodology can indicate not only the number of DG units, but also their type and their network location, in order to gain high performance when used with an appropriate OPF tool such as Plexos. Conversely, this approach could also be used to assist in the design of network topologies, working within the limitations of geography and socio-economic factors, by considering the connectedness of the network either by transmission line connection or by line capacity. For this network and the weather seen in the stated time period, it appears that wind-turbines may be the most important DG technology

to deploy, although the other types are important too since all wind DG would be unlikely to equal the performance seen, due not least to its intermittency.

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Fig. 6: ||-coords plot of the entire data set

For HC=70, showing the 72 variables, the derived *sumU* followed by the 4 objective functions. The best performing point of genCost is shown selected by the two arrows at the far right bottom, and its associated variables shown in blue when in colour. See Figure 7 for a clearer picture.

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Fig. 7: ||-coords plot of the entire data set

For HC=70, showing the 72 variables, the derived *sumU* followed by the 4 objective functions. The best performing point of genCost and its associated variables are shown, with the rest filtered out. The (W) annotation against a variable indicates that it is a Wind DG unit.

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